

# Differential gene expression analysis using RNA-seq

---

Applied Bioinformatics Core, November 2019

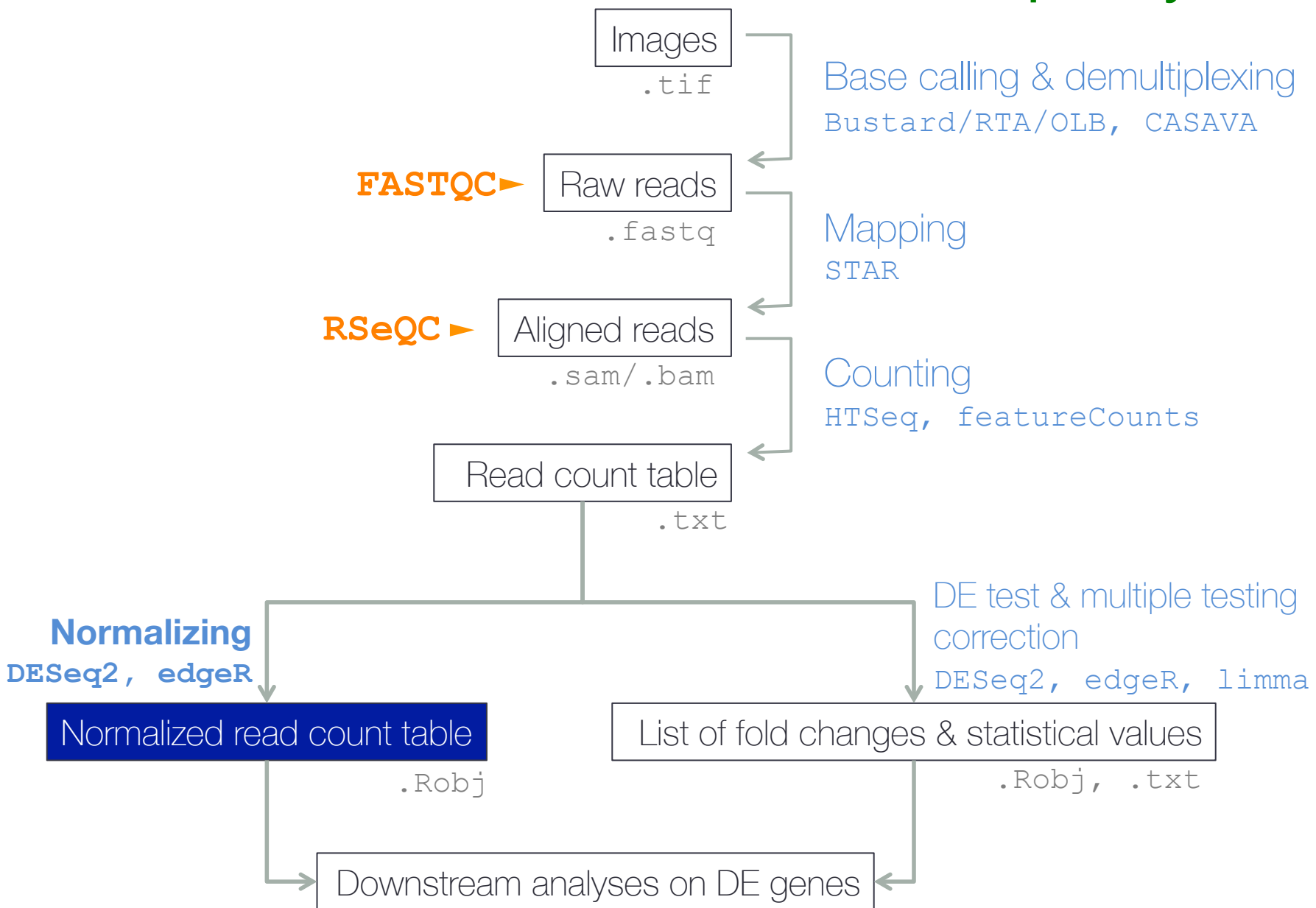


Friederike Dündar with Luce Skrabanek & Paul Zumbo

# Day 4 overview

- exploring read counts
  - rlog transformation
  - hierarchical clustering
  - PCA
- (brief) theoretical background for DE analysis
- DE analysis using DESeq2
- exploring the results

# Bioinformatics workflow of RNA-seq analysis



# featureCounts



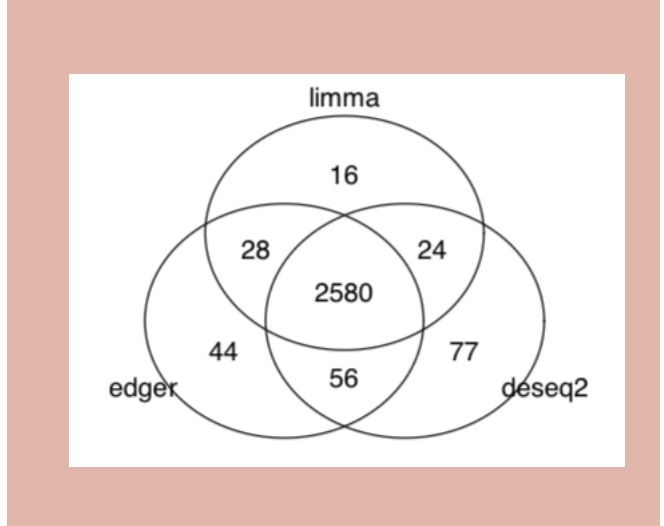
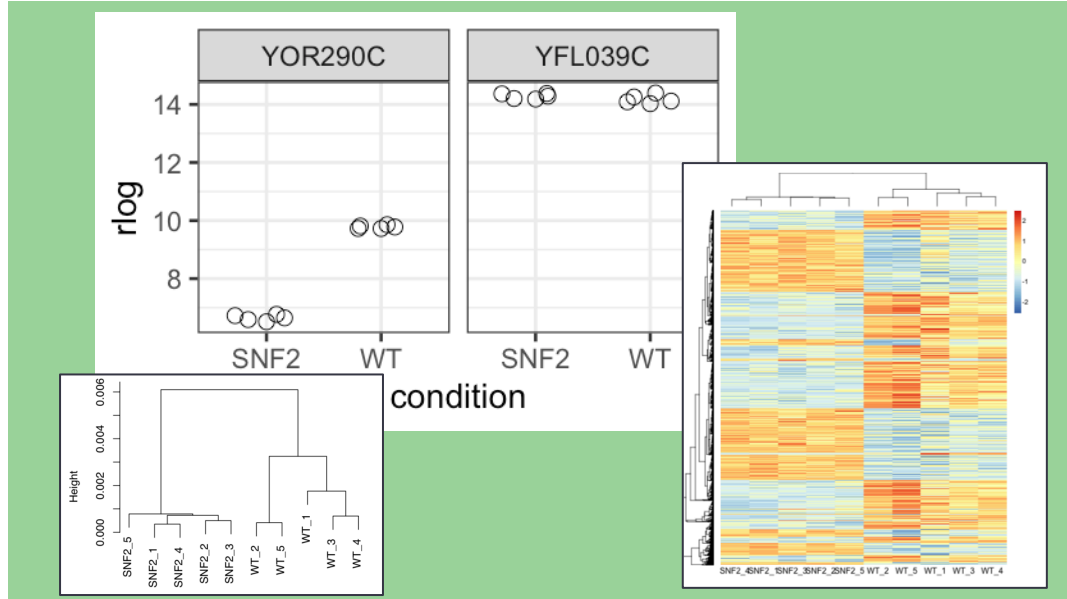
table of read counts  
(integers)

DESeq2/edgeR/limma  
functions for  
**normalizing**/rlog  
generation

exploratory analyses  
&  
visualizations

DESeq2/  
edgeR/limma  
functions for  
**DGE**

identifying genes with  
differential gene  
expression



# Expression units

- strongly influenced by

- gene length

- sequencing depth

- expression of all other genes in the same sample

DESeq's size factor normalization

- annoying mathematical properties of read counts

- large dynamic range

- discrete values

hetero-  
skedasticity

log transformation and variance stabilization (DESeq's  $\text{rlog}()$ )

Use **normalized and transformed** expression units for exploratory analyses!

# EXPLORATORY ANALYSES

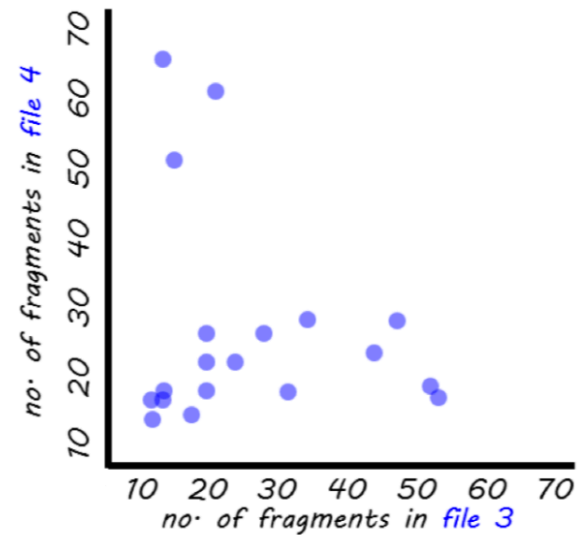
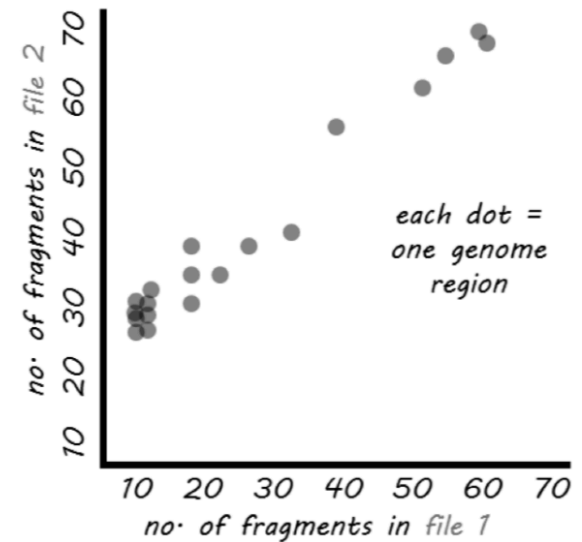
---

assessing sample similarities & sources of variation



# Pairwise correlation of gene expression values

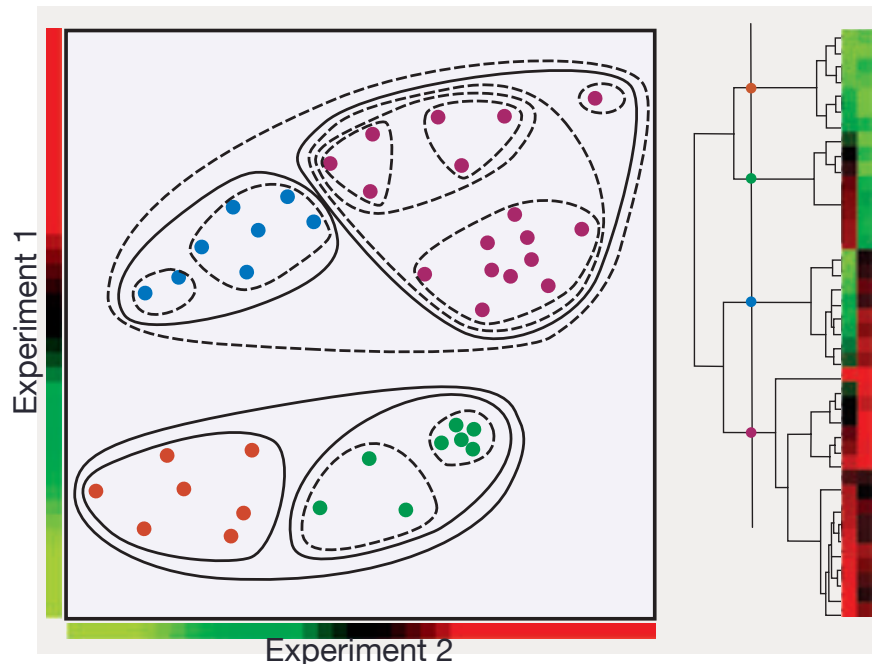
- replicates of the same condition should show high correlations ( $> 0.9$ )
- **Pearson** method: *metric* differences between samples
  - influenced by outliers
- **Spearman** method: based on *rankings*
  - less sensitive
  - less driven by outliers
- R function: `cor ( )`





# Clustering gene expression values

Goal: partition the samples into homogeneous groups such that the within-group similarities are large.



single-sample (or single-gene) clusters  
are successively joined

- + “unbiased”
- not very robust

- Result: dendrogram
  - clustering obtained by cutting the dendrogram at the desired level
- Similarity measures
  - Euclidean
  - Pearson correlation
- Distance measures
  - Complete: largest distance
  - Average: average distance

R function: `hclust()`

# PCA

starting point: matrix with expression values per gene and sample,  
e.g. 7,100 genes x 10 samples

	SNF2_1	SNF2_2	SNF2_3	SNF2_4	SNF2_5	WT_1	WT_2	WT_3	WT_4	WT_5
YDL248W	109	84	100	112	62	47	65	60	95	43
YDL247W.A	0	1	1	0	3	0	0	1	0	0
YDL247W	6	6	1	3	4	2	3	4	7	9
YDL246C	6	6	1	4	4	1	3	2	4	0
YDL245C	1	6	9	5	3	6	2	5	5	6
YDL244W	79	59	49	60	37	9	8	12	30	14

If we want to understand the main differences between SNF2 and WT samples, the most detailed view (with the most “dimensions”) would entail all 7,100 genes.

However, it is probably enough to focus on the genes that are actually different.

In fact, it’ll be even better if we could somehow identify entire groups of genes that capture the majority of the differences.

PCA does exactly that (“grouping genes”) using the correlation amongst each other.

	PC1	PC2
SNF2_1	-9.322866	0.8929154
SNF2_2	-9.390920	-0.6478100
SNF2_3	-9.176814	0.3460428
SNF2_4	-9.693035	1.2174519
SNF2_5	-9.450847	-0.3668670
WT_1	8.378671	-6.3321623
WT_2	10.421518	4.6749399
WT_3	8.486379	-1.1793146
WT_4	8.517490	-4.5814481
WT_5	11.230425	5.9762519

2 PCs (or more) x 10 samples

# Principal component analysis

Goal: Reduce the dataset to fewer dimensions yet approx. preserve the distance between the individual samples

**starting point:** matrix with expression values per gene and sample, e.g. 7,100 genes x 10 samples

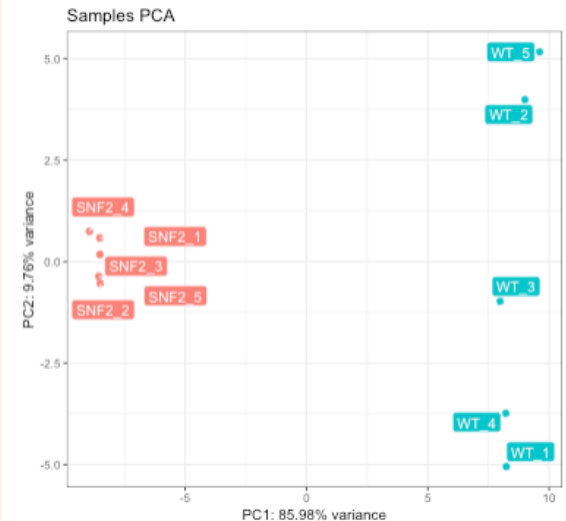
	SNF2_1	SNF2_2	SNF2_3	SNF2_4	SNF2_5	WT_1	WT_2	WT_3	WT_4	WT_5
YDL248W	109	84	100	112	62	47	65	60	95	43
YDL247W.A	0	1	1	0	3	0	0	1	0	0
YDL247W	6	6	1	3	4	2	3	4	7	9
YDL246C	6	6	1	4	4	1	3	2	4	0
YDL245C	1	6	9	5	3	6	2	5	5	6
YDL244W	79	59	49	60	37	9	8	12	30	14



**7,100 principal components x 10 samples**

- vectors along which the variation between samples is maximal
- PC1-3 usually sufficient to capture the major trends!

	PC1	PC2
SNF2_1	-9.322866	0.8929154
SNF2_2	-9.390920	-0.6478100
SNF2_3	-9.176814	0.3460428
SNF2_4	-9.693035	1.2174519
SNF2_5	-9.450847	-0.3668670
WT_1	8.378671	-6.3321623
WT_2	10.421518	4.6749399
WT_3	8.486379	-1.1793146
WT_4	8.517490	-4.5814481
WT_5	11.230425	5.9762519

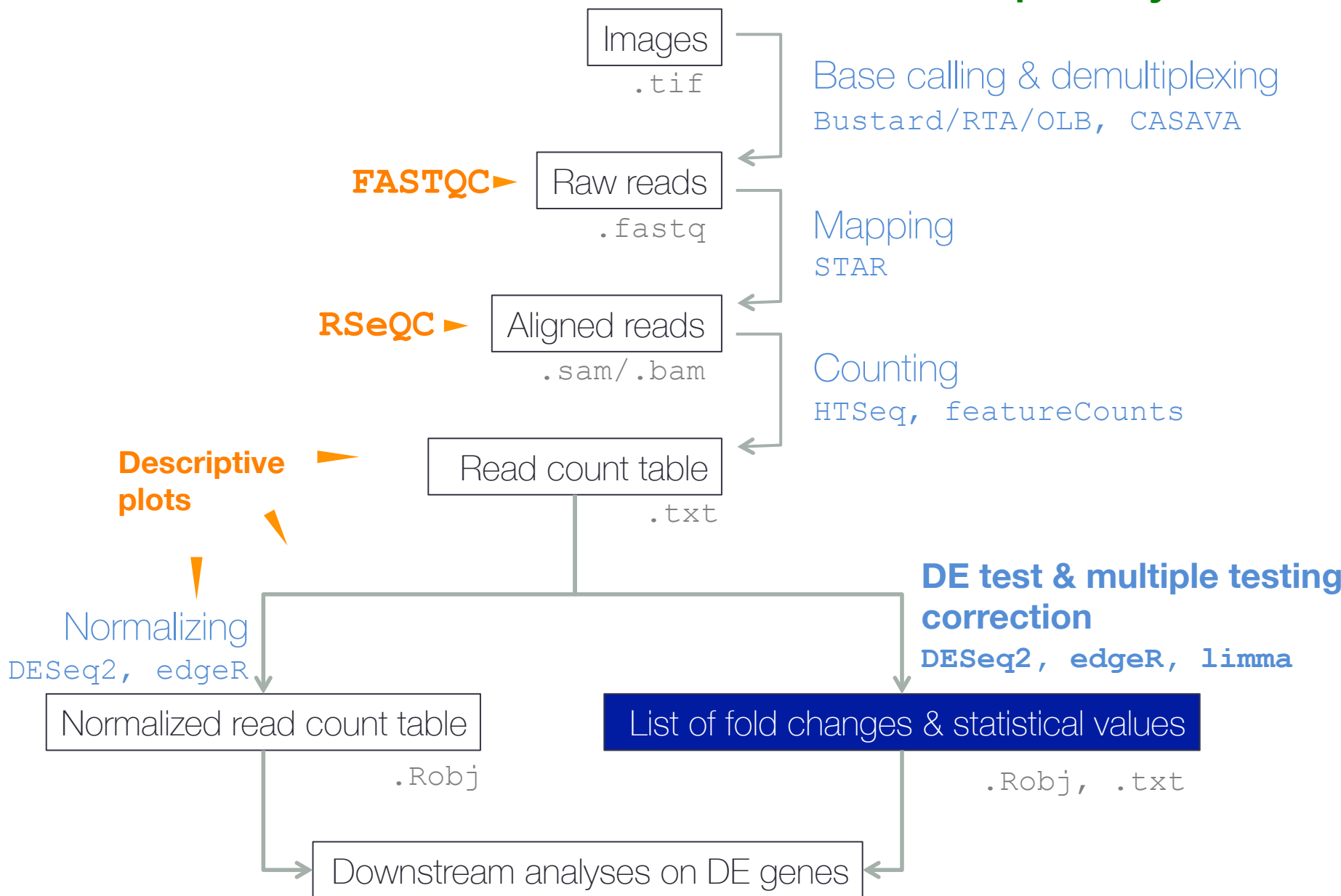


# DIFFERENTIAL GENE EXPRESSION

---

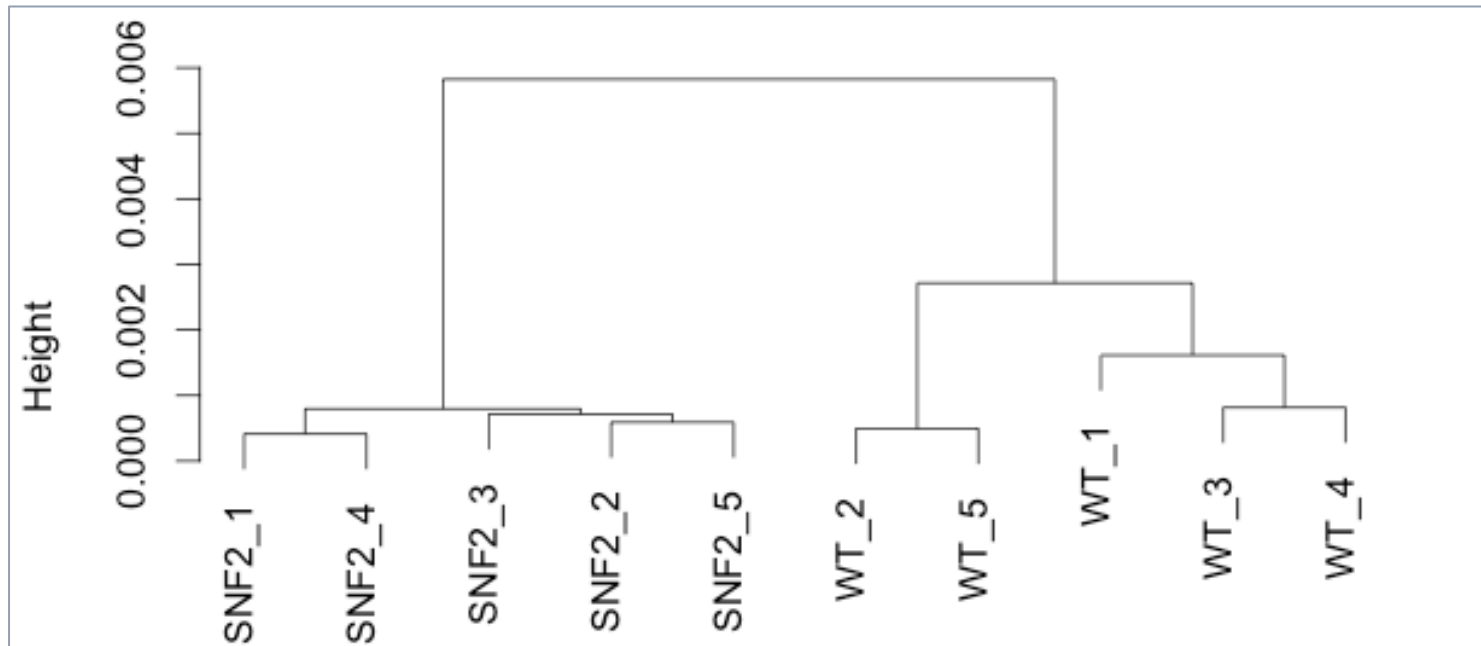
Identifying genes with statistically significant expression differences between samples of different conditions

# Bioinformatics workflow of RNA-seq analysis

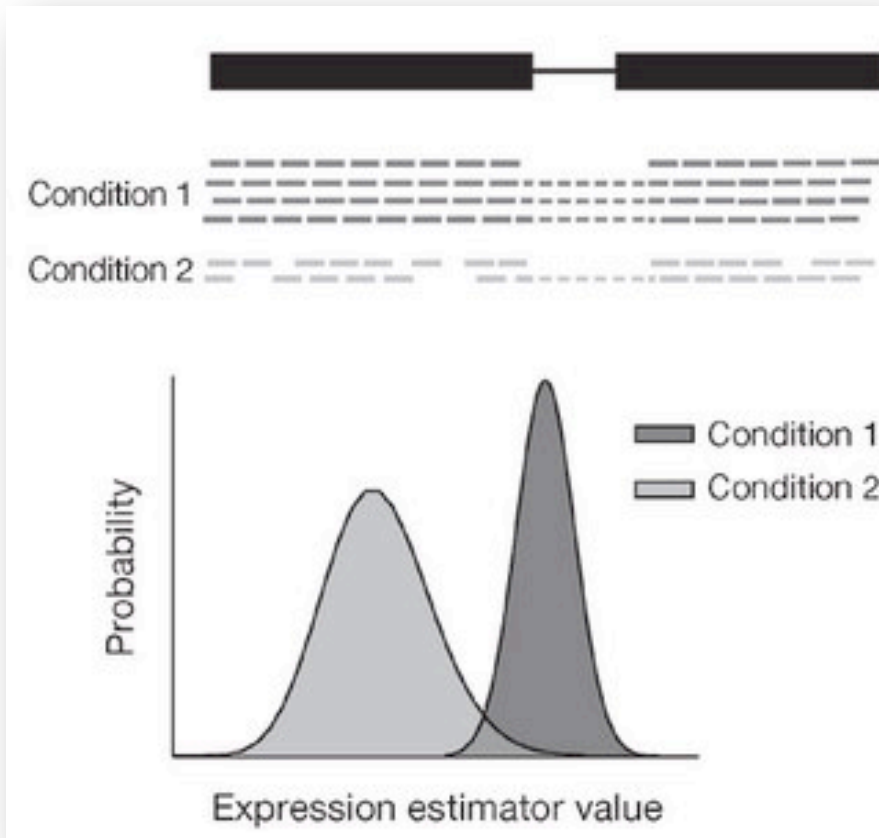


# Read count table

	SNF2_1	SNF2_2	SNF2_3	SNF2_4	SNF2_5	WT_1	WT_2	WT_3	WT_4	WT_5
YAL012W	7347	7170	7643	8111	5943	4309	3769	3034	5601	4164
YAL068C	2	2	2	1	0	0	0	0	2	2
YAL067C	103	51	44	90	53	12	23	21	30	29
YAL066W	2	0	0	0	0	0	0	0	0	0
YAL065C	5	9	6	3	1	10	5	2	4	3
YAL064W-B	13	9	10	9	6	9	12	4	4	8



# DE basics



1 test per gene!

1. Estimate **magnitude** of DE taking into account differences in sequencing depth, technical, and biological read count variability.

logFC

2. Estimate the **significance** of the difference accounting for performing thousands of tests.

(adjusted)  
p-value

*H<sub>0</sub>: no difference in the read distribution between two conditions*

# Estimating the difference with regression models

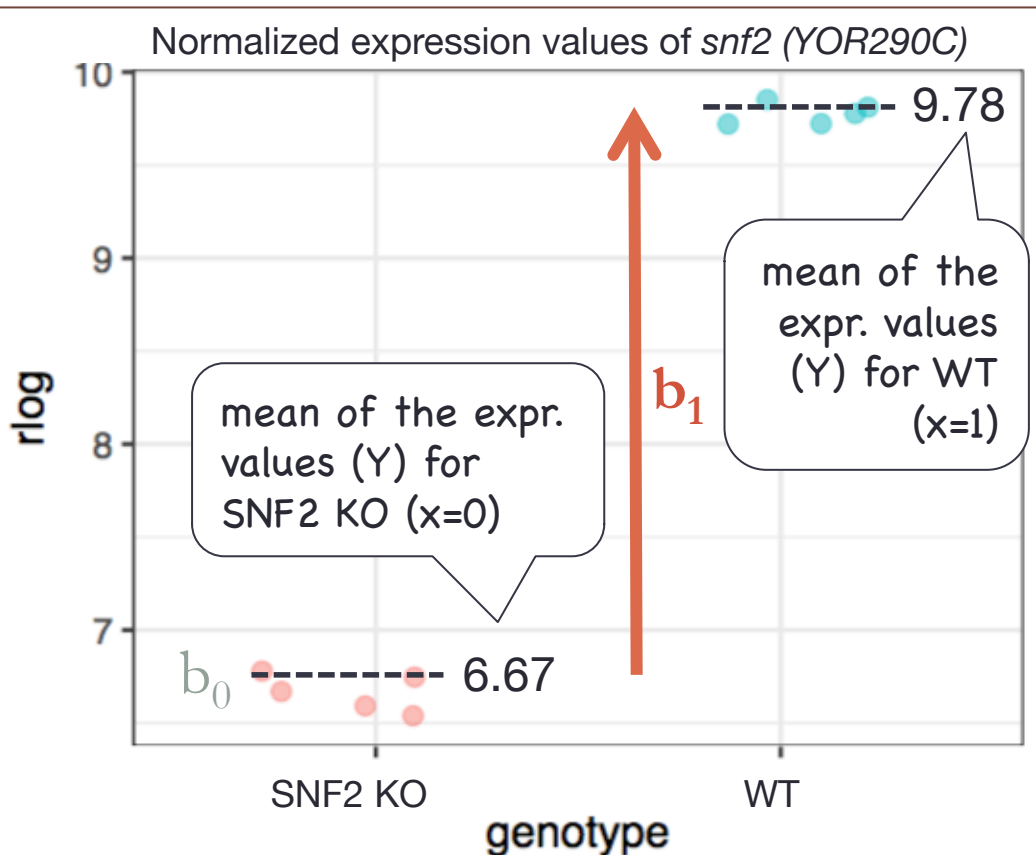
**Example:** Modeling normalized gene expression values using a linear model

describing all normalized expression values of one example gene using a simple linear model of the following form:

$$Y = b_0 + b_1 * x + e$$

expr. values    intercept    **delta**    genotype

$b_0$ : **intercept**, i.e. average of the baseline group  
 $b_1$ : **difference** between baseline & non-reference group  
 $x$  : 0 if genotype == "SNF2", 1 if genotype == "WT"



```
# 1. FIT the model  
> lmfit <- lm(rlog.norm ~ genotype)  
# 2. ESTIMATE the coefficients  
> coef(lmfit)
```

(Intercept)	genotypeWT	$b_1$
6.666	3.111	
$b_0$	$b_1$	

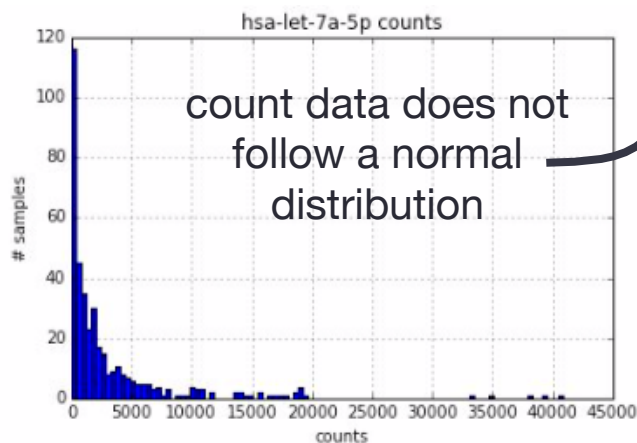
both beta values are **estimates!**

(they're spot-on because the data is so clear for this example and the model is so simple)



# DE analysis: dealing with raw read counts

1. **Fitting** a sophisticated model (not a basic linear model) to get a grip on the read counts (done per gene; includes normalization)
  - library size factor
  - dispersion estimate using information across multiple genes
  - assuming a neg. binomial distribution of read counts



negative binomial (NB) model

$$K_{ij} \sim \text{NB}(\mu_{ij}, \alpha_i)$$

read counts for gene  $i$  and sample  $j$

gene-specific dispersion parameter (fitted towards the average dispersion)

mean expr.

library size factor

$$\mu_{ij} = s_j q_{ij}$$

# DE analysis

1. **Fitting** a sophisticated model to get a grip on the read counts (done per gene; includes normalization)

$$K_{ij} \sim \text{NB}(\mu_{ij}, \alpha_i)$$

read counts for gene  $i$  and sample  $j$

gene-specific dispersion parameter (fitted towards the average dispersion)

mean expr.

library size factor

$$\mu_{ij} = s_j q_{ij}$$

2. Estimating **coefficients** of the model to obtain the difference between the estimated mean expression of the different groups (log2FC)
  - define the **contrast of interest**, e.g.  $\sim$  batchEffect + condition
  - always put **the factor of interest last**
  - order of the factor levels determines the direction of log2FC

# DE analysis

1. **Fitting** a sophisticated model to get a grip on the read counts (done per gene; includes normalization)

$$K_{ij} \sim \text{NB}(\mu_{ij}, \alpha_i)$$

read counts for gene  $i$  and sample  $j$       mean expr.      library size factor

gene-specific dispersion parameter (fitted towards the average dispersion)

$$\mu_{ij} = s_j q_{ij}$$

2. Estimating **coefficients** of the model to obtain the difference between the estimated mean expression of the different groups (log2FC)
3. **Test** whether the log2FC is “far away” from 0
  - log-likelihood test or Wald test are used by DESeq2
  - multiple hypothesis test correction

# Modeling read counts and estimating the log<sub>2</sub>-fold-change (DESeq2)

$$K_{ij} \sim \text{NB}(\overset{\text{fitted mean}}{\mu_{ij}}, \overset{\text{gene-specific dispersion parameter}}{\alpha_i} \text{ (fitted towards the average dispersion)})$$

read counts for gene  $i$  and sample  $j$

$$\mu_{ij} = s_j q_{ij}$$

library size factor

expression value estimate

moderated log-fold change for gene  $i$

$$\log_2(q_{ij}) = x_j \cdot \beta_i$$

model matrix column for sample  $j$

Once the coefficients are estimated, the significance tests need to test how far away from zero they are since zero would mean “no difference”.

*H<sub>0</sub>: no difference in the read distribution between two conditions*

**Let's do this!**

# From read counts to DE

	SNF2_1	SNF2_2	SNF2_3	SNF2_4	SNF2_5	WT_1	WT_2	WT_3	WT_4	WT_5
YAL012W	7347	7170	7643	8111	5943	4309	3769	3034	5601	4164
YAL068C	2	2	2	1	0	0	0	0	2	2
YAL067C	103	51	44	90	53	12	23	21	30	29
YAL066W	2	0	0	0	0	0	0	0	0	0
YAL065C	5	9	6	3	1	10	5	2	4	3
YAL064W-B	13	9	10	9	6	9	12	4	4	8

`DESeq2::DESeq(ds_object)`



	baseMean	log2FoldChange	lfcSE	stat	pvalue	padj
	<numeric>	<numeric>	<numeric>	<numeric>	<numeric>	<numeric>
YAL012W	5538.0476736	-0.3049727	0.1564379	-1.9494807	5.123804e-02	1.002376e-01
YAL068C	0.9677468	-0.1306360	0.3922204	-0.3330679	7.390830e-01	NA
YAL067C	40.8756727	-1.0144579	0.2128597	-4.7658520	1.880572e-06	1.145269e-05
YAL066W	0.1403184	-0.1343829	0.1806512	-0.7438804	4.569489e-01	NA
YAL065C	5.1638597	0.3447455	0.4060259	0.8490726	3.958409e-01	5.083659e-01
YAL064W-B	8.4455750	0.1250101	0.3437285	0.3636887	7.160905e-01	7.906075e-01

average  
norm.  
count

standard error  
estimate for the  
logFC

# Exploratory vs. DE analysis workflow

raw reads

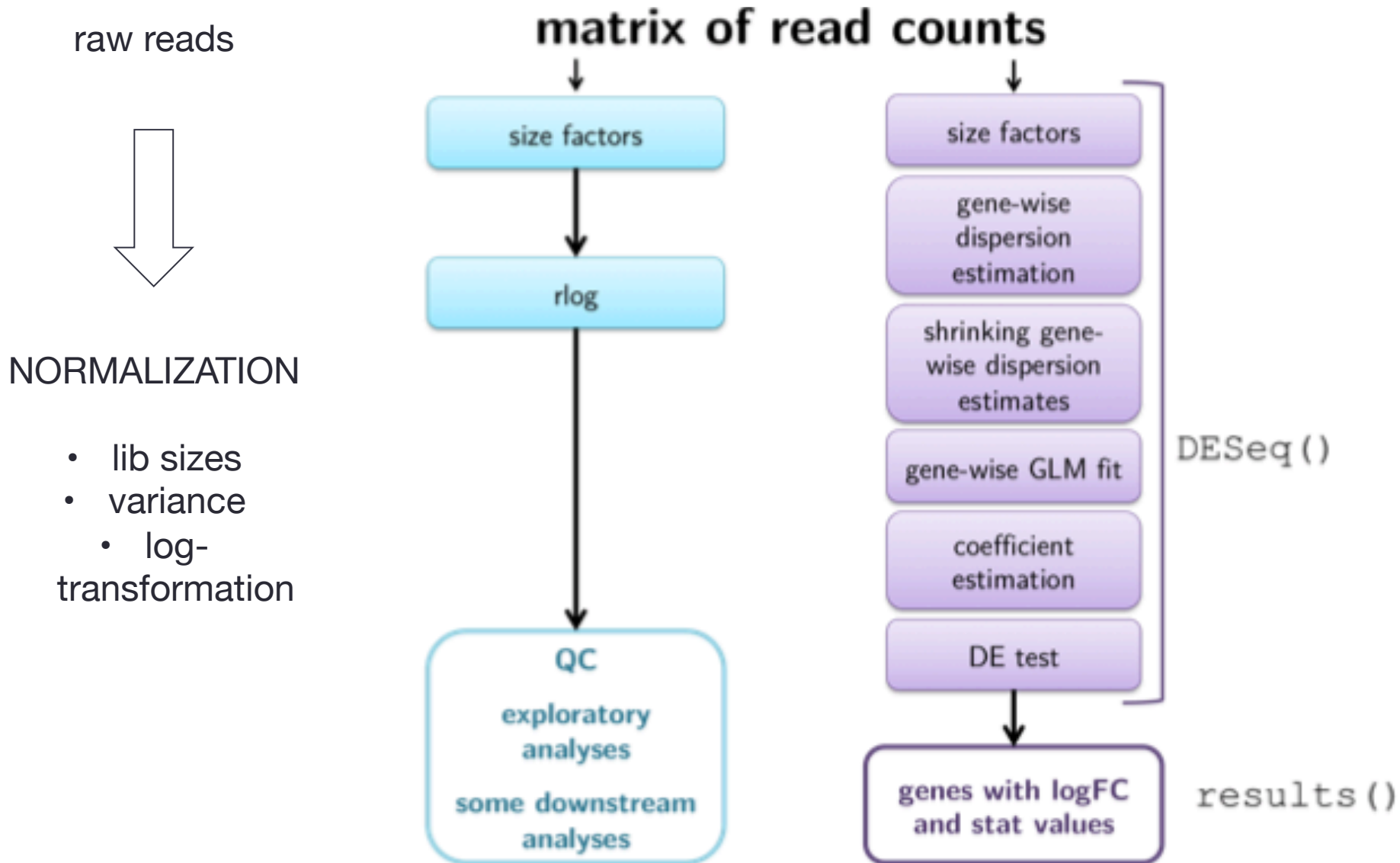


NORMALIZATION

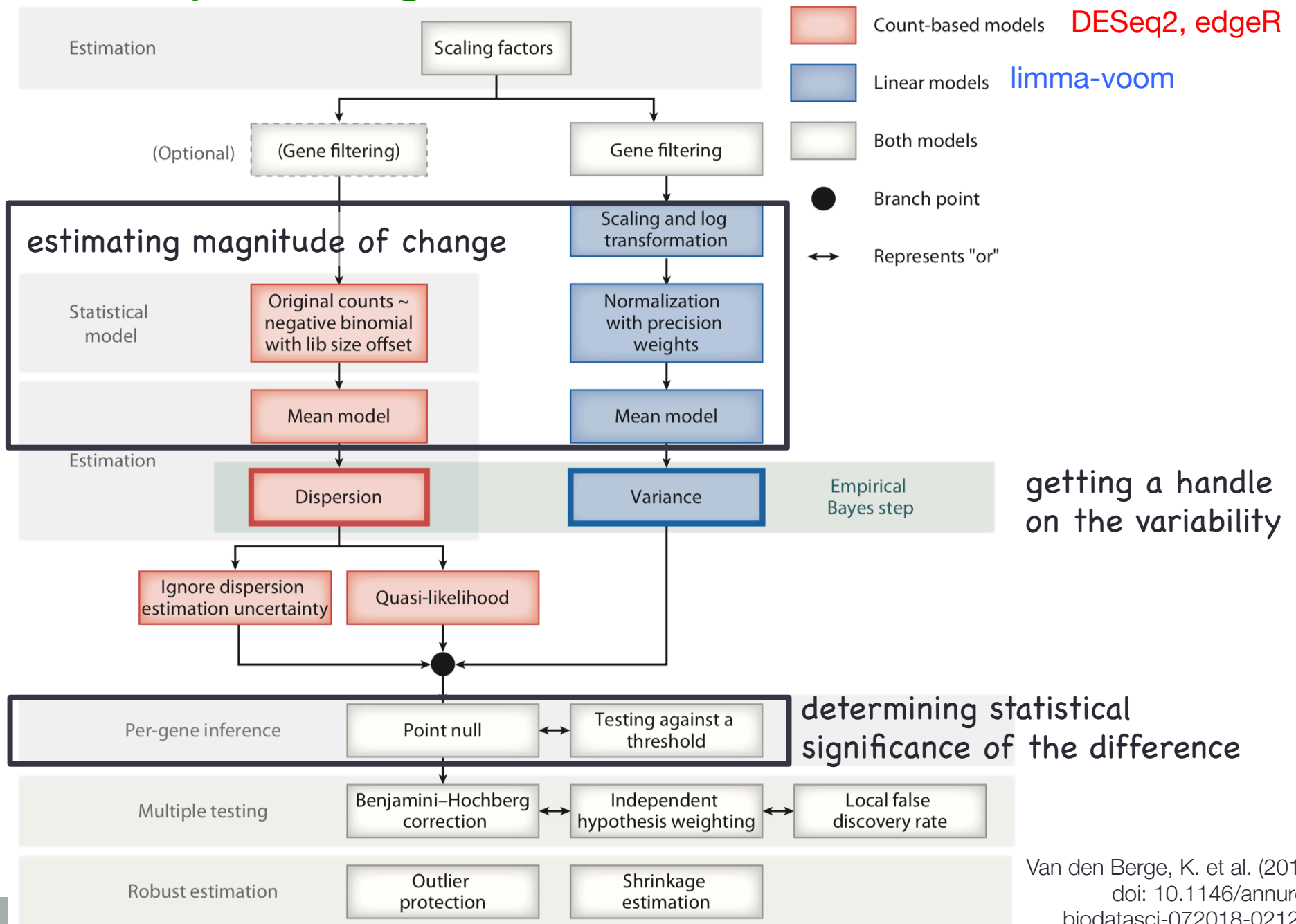
- lib sizes
- variance
- log-transformation



# Exploratory vs. DE analysis workflow



# DESeq2 vs. edgeR vs. limma-voom





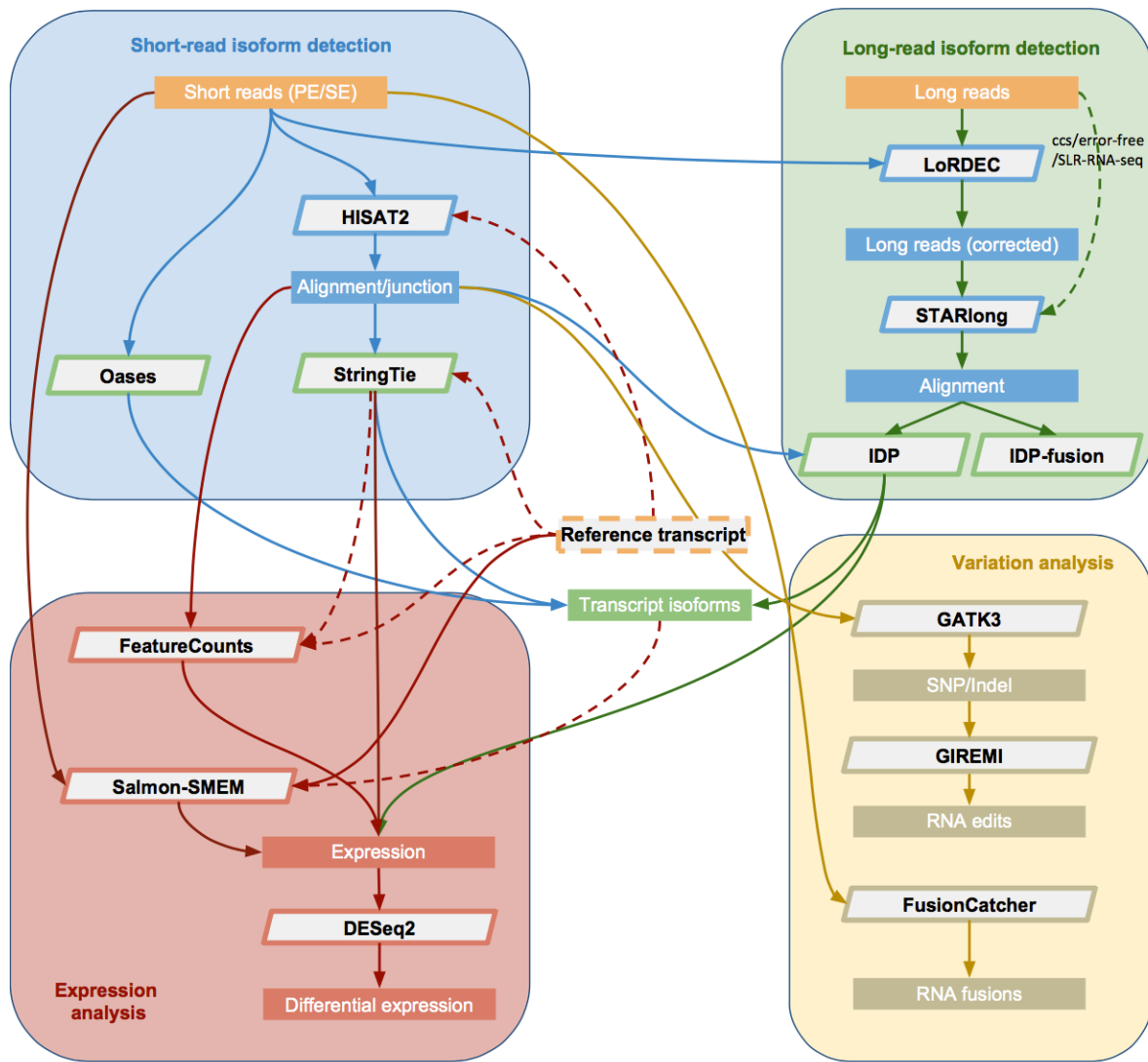
# What next?

- Do your results make sense?
- Are the results robust?
  - do **multiple tools** agree on the majority of the genes?
  - are **the fold changes** strong enough to explain the phenotype you are seeing?
  - have **other experiments** yielded similar results?
- Downstream analyses: mostly **exploratory**

## How to decide which tool(s) to use?

- function/content of original publication
  - code maintained?
  - well documented?
  - used by others?
    - efficient?

# RNACocktail tries to implement all (current!) best performers for various RNA-seq analyses



Task	Command
Short-read alignment	align
Short-read transcriptome reconstruction	reconstruct
Short-read quantification	quantify
Short-read differential expression	diff
Short-read de novo assembly	denovo
Long-read error correction	long_correct
Long-read alignment	long_align
Long-read transcriptome reconstruction	long_reconstruct
Long-read fusion detection	long_fusion
Variant calling	variant
RNA editing detection	editing
RNA Fusion detection	fusion
Running all steps	all

# Where to get help and inspiration?

[bioconductor.org/help/workflows](http://bioconductor.org/help/workflows)

## F100Research Software Tool Articles

Periodic Table of Bioinformatics:  
<http://elements.eaglegenomics.com/>

mailing lists/github issues of the  
individual tools

[biostars.org](http://biostars.org)

[seqanswers.com](http://seqanswers.com)

[stackoverflow.com](http://stackoverflow.com)

Picardi: RNA Bioinformatics (2015)  
<https://www.springer.com/us/book/9781493922901>

supplemental material of publications based on HTS data

## WALK-IN CLINICS

@ **WCM:**

Thursdays, 1:30 – 3 pm,  
LC-504 (1300 York Ave)

[abc.med.cornell.edu](http://abc.med.cornell.edu)

@ **MSKCC:**

[https://www.mskcc.org/  
research-advantage/core-  
facilities/bioinformatics](https://www.mskcc.org/research-advantage/core-facilities/bioinformatics)

<https://github.com/abctdbug/dbug>

# Everything's connected...

## Sample type & quality

- Low input?
- Degraded?

## Experimental design

- Controls
- No. of replicates
- Randomization

## Library preparation

- Poly-A enrichment vs. ribo minus
- Strand information

## Biological question

- Expression quantification
- Alternative splicing
- De novo assembly needed
- mRNAs, small RNAs
- ....

## Sequencing

- Read length
- PE vs. SR
- Sequencing errors

## Bioinformatics

- Aligner
- Annotation
- Normalization
- DE analysis strategy